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Equations of Circles

Equation of a Circle:

$$(x-h)^2 + (y-k)^2 = r^2$$

x, y stay

(h, k) center

r: radius

Ex: Find the center and radius.

$$(x - 2)^2 + (y + 4)^2 = 16$$

center: $(2, -4)$

radius: 4

Write the equation for each circle...

Ex: center (- 3, 6) , radius $\sqrt{5}$

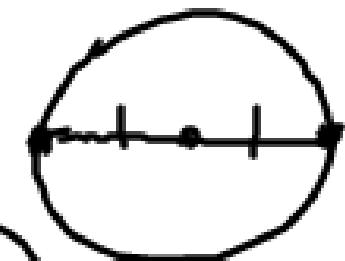
$$(x + 3)^2 + (y - 6)^2 = 5$$

Write the equation for each circle...

Ex: diameter has endpoints
(-7, -2) and (-15, 6)

center: $(-11, 2)$ $\left(\frac{-7 + -15}{2}, \frac{-2 + 6}{2} \right)$

radius: $\sqrt{32}$



$$d = \sqrt{(-11 + 7)^2 + (2 + 2)^2}$$

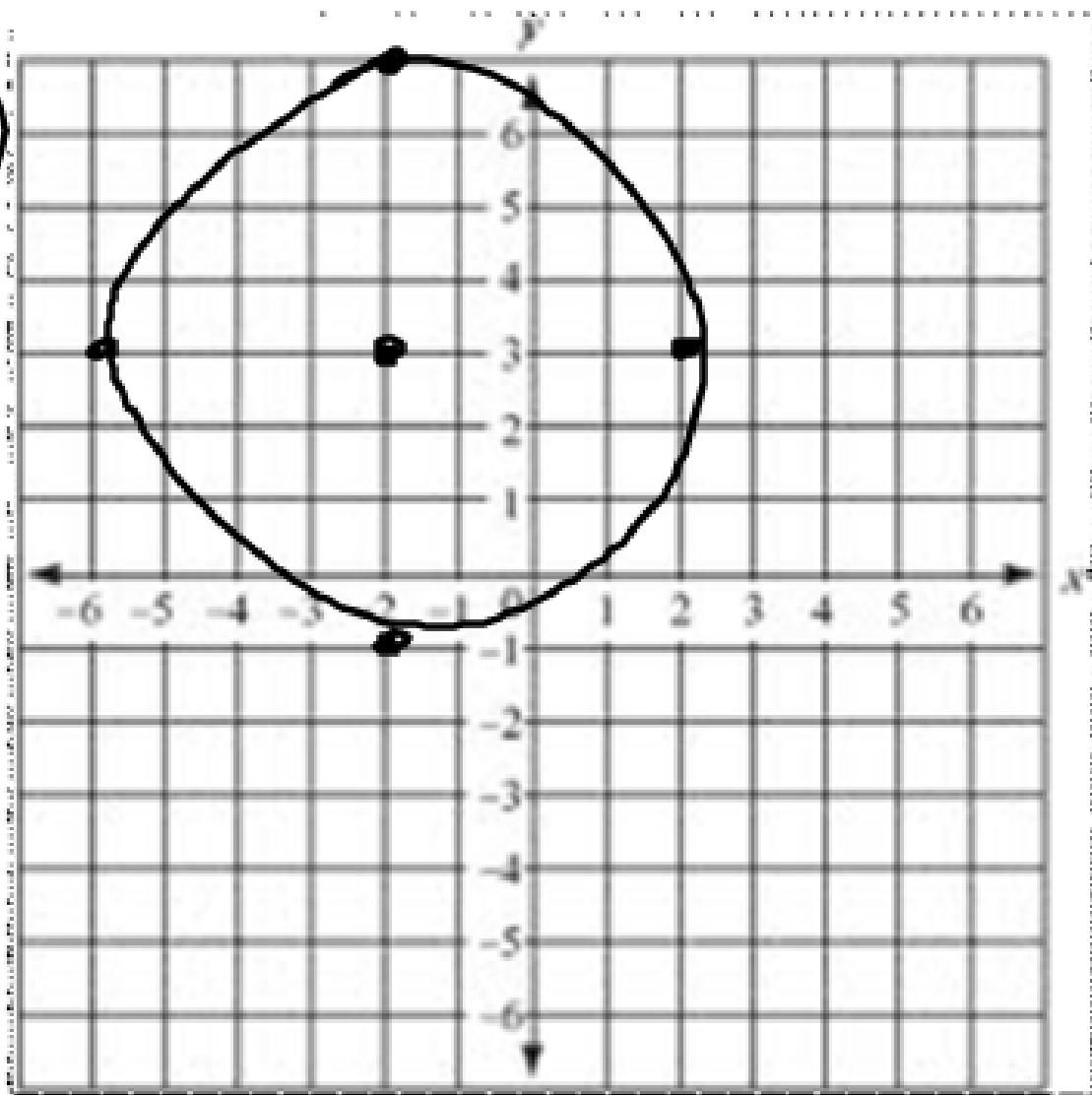
$$\sqrt{16 + 16} = \sqrt{32}$$

$$(x + 11)^2 + (y - 2)^2 = 32$$

Ex: Graph $(x + 2)^2 + (y - 3)^2 = \sqrt{16}$.

center: $(-2, 3)$

radius: 4



Ex: Graph $x^2 + y^2 = 9$.

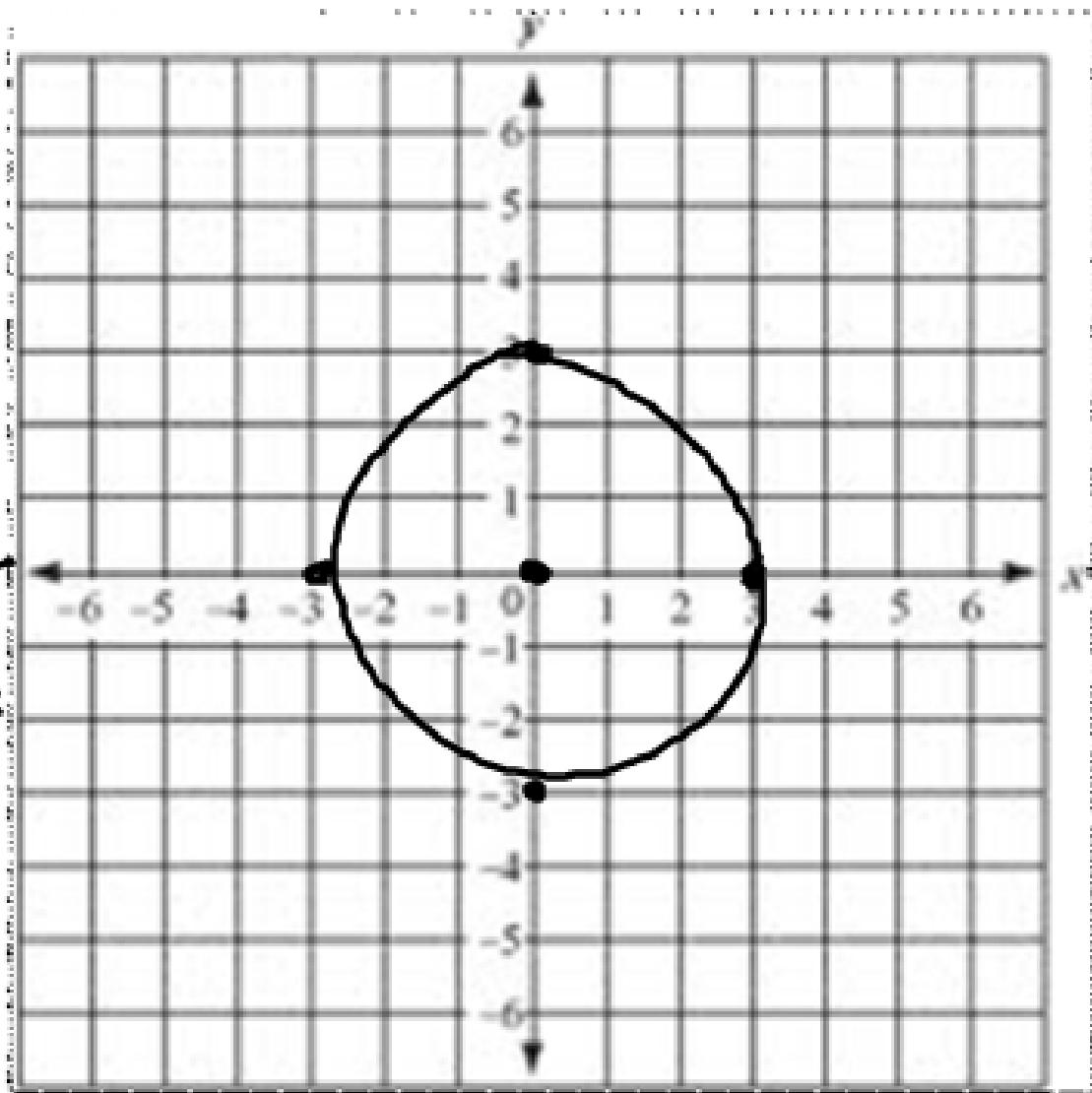
$$(x \cancel{=} \cancel{3})^2 + (y \cancel{=} \cancel{3})^2 = 9$$

$(0, 0)$

$r: 3$

$$\text{---} (x - 0)^2 + (y + 3)^2 =$$

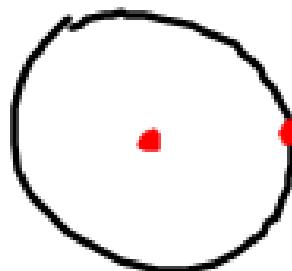
$$x^2 + (y + 3)^2 =$$



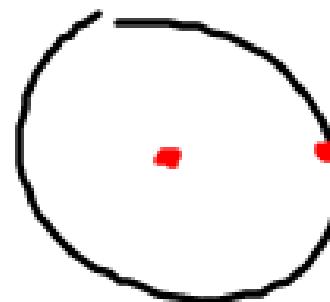
midpoint $\left(\frac{x+x}{2}, \frac{y+y}{2} \right)$

distance $d = \sqrt{(x-x)^2 + (y-y)^2}$

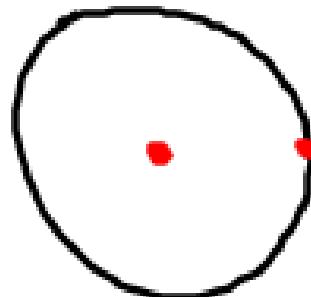
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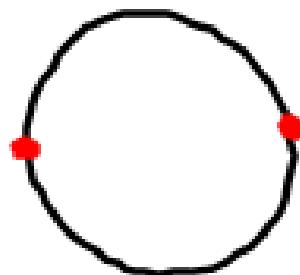
8.)



9.)



10.)



Homework:

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